## Get a Half-Life!: Student Worksheet

Name:
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A decay function is one in which the values decrease by a constant factor, but it is not linear! These functions are often used to model the decay of a radioactive element. The half-life of a substance is the time it takes to reduce its initial effectiveness by one-half.

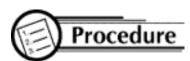
## Group Arrangement

Students work in pairs



Each pair needs:

- 1 cup of *m&m*'s
- 1 paper plate or box
- 1 graphing calculator



#### A. Collect the Data

- 1. Pour m&m's out and count your beginning sample size (N). This will be your N value when T = 0. Enter this value in the table below and put the m&m's back in the cup.
- 2. Shake the cup gently and pour the m&m's out in the box or on the paper plate.
- 3. Remove all the m&m's with an "m" showing. (You may eat these m&m's only!)

- 4. Count the remaining m&m's and enter this value of N into your table next to T = 1.
- 5. Put the remaining m&m's back in the cup.
- 6. Repeat this process until there are no longer any m&m's with the letter "m" when you empty your cup.

Trial Number	0	1	2	3	4	5	6	7
<b>(T)</b>								
# of remaining								
<i>m&amp;m</i> 's (N)								

#### B. Use the Calculator

1. Clear out the calculator:

Press [2<sup>nd</sup>][Y=]. Enter [4]. Press [ENTER]. This turns off all plots.

Press [Y=], [CLEAR], down arrow and [CLEAR] until all equations are cleared.

Press [STAT], [ENTER] to view tables. To clear Lists, press up arrow to highlight L1, press [CLEAR],

[ENTER]. Use arrow keys to highlight any other lists and clear.

2. Enter the data from the table above:

Press [STAT], choose EDIT by pressing [ENTER] and enter values of T in L1 using down arrow keys and [ENTER].

Use right arrow key to move over to L2 and enter the values of N in L2.

3. Graph the Data

Press [STAT PLOT] ([2<sup>nd</sup>][Y=]), choose 1 by pressing [ENTER].

Highlight: ON

Broken line graph

Xlist: L1 Ylist: L2

Mark: first one

Press [ZOOM], then [9] to set up appropriate window and see graph.

4. Have the calculator determine the best equation for the data.

#### Linear:

Press [STAT]. Choose CALC[5].

Type in L1, L2 (press [2<sup>nd</sup>][1][,][2<sup>nd</sup>][2] then

[ENTER]). You will see y = ax + b and values for a, b, and r.

Press [Y=], set cursor next to Y1=, press [VARS][5], arrow over to EQ, press [7], the [GRAPH].

## **Quadratic:**

Press [STAT], choose CALC [6], then type in L1, L2 (like above) and press [ENTER].

Press [Y=]. Set your cursor next to Y2=.

Press [VARS][5], arrow over to EQ, press [7], the [GRAPH]. (Adjust the window here to see more of this graph)

## **Exponential:**

Press [STAT] and choose CALC. Choose A by using the down arrow key until you see "A ExpReg". Press [ENTER].

Type in L1, L2 as before and then [ENTER]. You will see  $y = a*b^x$  ( $y = ab^x$ ) and values for a, b, and r. Press [Y=] and set your cursor next to Y3=. Press [VARS], choose [5], arrow over to EQ, press [7], then [GRAPH].

## C. Analyze the Data

- 1. Which graph most clearly approximates a "curve of best fit" for your data?
- 2. Why is this called a "half-life"?
- 3. What is a good estimate for the length of a "half-life" of *m&m*'s based on your research?

# Math Connection

As a result of this activity, students learn to model a real-life situation by collecting data from a few trials, graphing the data, and then drawing a curve of best fit. The student must decide which of the equations best fits his/her data. Sometimes when a student gathers his/her own data, the graph does not make a perfect line or curve.



- Describe the factors that influenced you to choose your "curve of best fit".
- 2. Explain how each of the three types of equations, linear, quadratic, and exponential, are different.